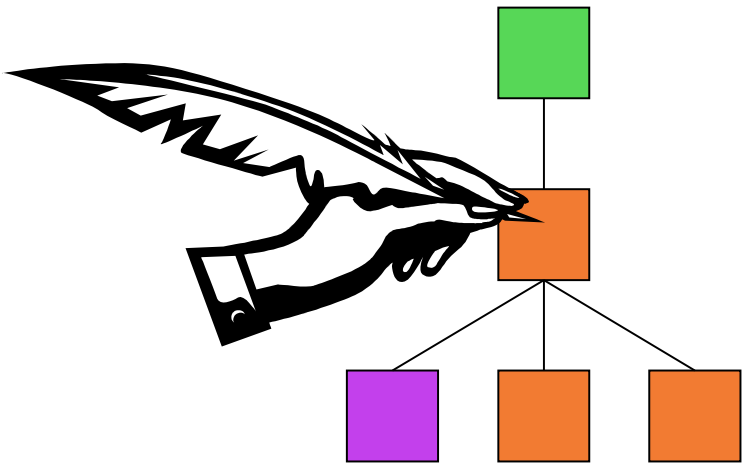


# $\lambda$ Playing with Haskell Data

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# $\lambda$ Overview

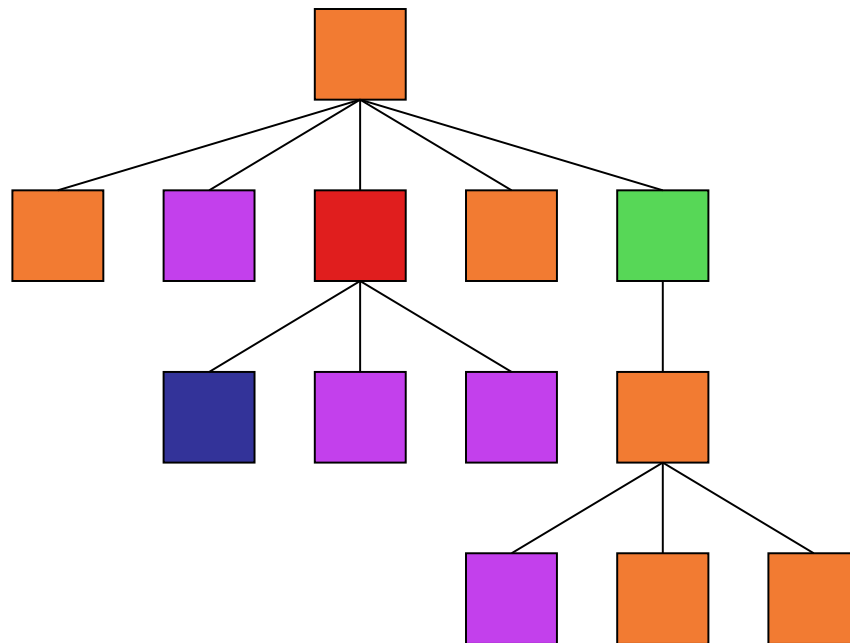
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- The “boilerplate” problem
- Haskell’s weakness (really!)
- Traversals and queries
- Generic traversals and queries
- Competitors (SYB and Compos)
- Benchmarks

# λ Data structures

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- A tree of *typed* nodes
- Parent/child relationship is important



# A concrete data structure

---

```
data Expr = Val Int
          | Neg Expr
          | Add Expr Expr
          | Sub Expr Expr
```

- Simple arithmetic expressions

# $\lambda$ Task: Add one to every Val

```
inc :: Expr -> Expr
```

```
inc (Val i) = Val (i+1)
```

```
inc (Neg x) = Neg (inc x)
```

```
inc (Add x y) = Add (inc x) (inc y)
```

```
inc (Sub x y) = Sub (inc x) (inc y)
```

- What is the worst thing about this code?

# $\lambda$ Many things!

---

1. If we add Mul, we need to change
2. The action is one line, obscured
3. Tedious, repetitive, dull
4. May contain subtle bugs, easy to overlook
5. Way too long

# $\lambda$ The boilerplate problem

---

- A lot of tasks:
  1. Navigate a data structure (boilerplate)
  2. Do something (action)
- Typically boilerplate is:
  - Repetitive
  - Tied to the data structure
  - Much bigger than the action

# $\lambda$ Compared to Pseudo-OO<sup>1</sup>

```
class Expr
class Val : Expr {int i}
class Neg : Expr {Expr a}
class Add : Expr {Expr a, b}
class Sub : Expr {Expr a, b}
```

1) Java/C++ are way to verbose to fit on slides!



# Inc, in Pseudo-OO

---

```
void inc(x) {  
  if (x is Val) x.i += 1;  
  if (x is Neg) inc(x.a)  
  if (x is Add) inc(x.a); inc(x.b)  
  if (x is Mul) inc(x.a); inc(x.b)  
}
```

Casts, type evaluation etc omitted

# $\lambda$ Haskell's weakness

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- OO actually has a lower complexity
  - Hidden very effectively by horrible syntax
- In OO objects are deconstructed
- In Haskell data is deconstructed *and* reconstructed
- OO destroys original, Haskell keeps original

# $\lambda$ Comparing inc for Add

- Haskell

```
inc (Add x y) = Add (inc x) (inc y)
```

- OO

```
if (x is Add) inc(x.a); inc(x.b)
```

- Both deconstruct Add (follow its fields)
- Only Haskell rebuilds a new Add

# $\lambda$ Traversals and Queries

---

- What are the common forms of “boilerplate”?
  - Traversals
  - Queries
- Other forms do exist, but are far less common

# Traversals

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- Move over the entire data structure
- Do “action” to each node
- Return a new data structure
  
- The previous example (inc) was a traversal

# $\lambda$ Queries

---

- Extract some information out of the data
- Example, what values are in an expression?

# $\lambda$ A query

---

```
vals :: Expr -> [Int]
```

```
vals (Val i) = [i]
```

```
vals (Neg x) = vals x
```

```
vals (Add x y) = vals x ++ vals y
```

```
vals (Mul x y) = vals x ++ vals y
```

- Same issues as traversals

# $\lambda$ Generic operations

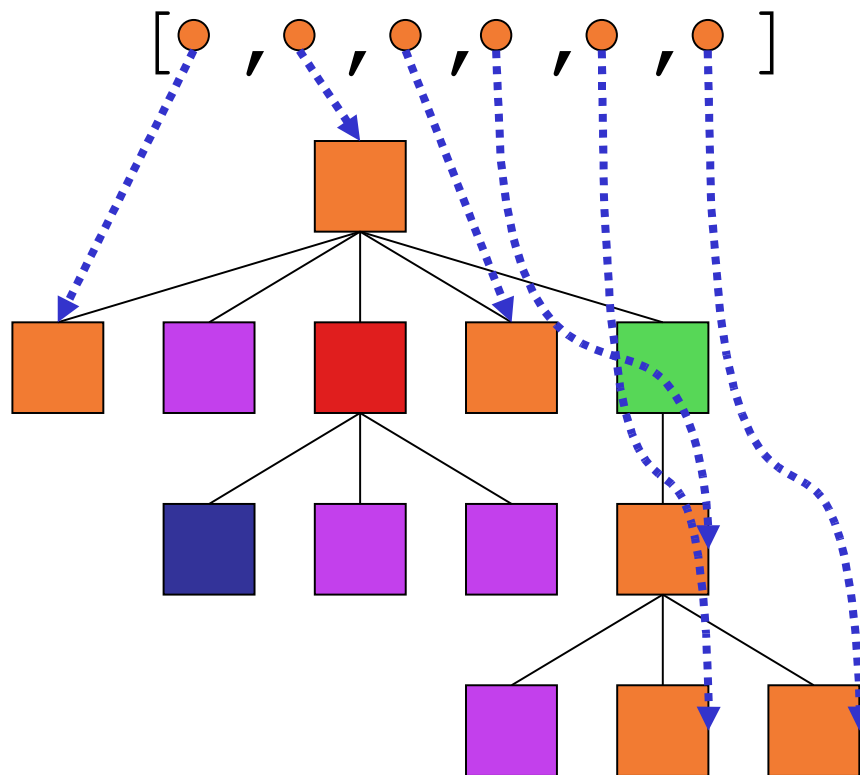
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- Identify primitives
  - Support lots of operations
  - Neatly
  - Minimal number of primitives
- These goals are in opposition!
- Here follow my basic operations...



# $\lambda$ Generic Queries

`allOver :: a -> [a]`



# $\lambda$ The vals query

---

```
vals x = [i | Val i <- allOver x]
```

- Uses Haskell list comprehensions – very handy for queries
- Can anyone see a way to improve on the above?
- Short, sweet, beautiful 😊

## $\lambda$ More complex query

---

- Find all negative literals that the user negates:

```
[i | Neg (Val i) <- allOver x  
  , i < 0]
```

- Rarely gets more complex than that

# $\lambda$ Generic Traversals

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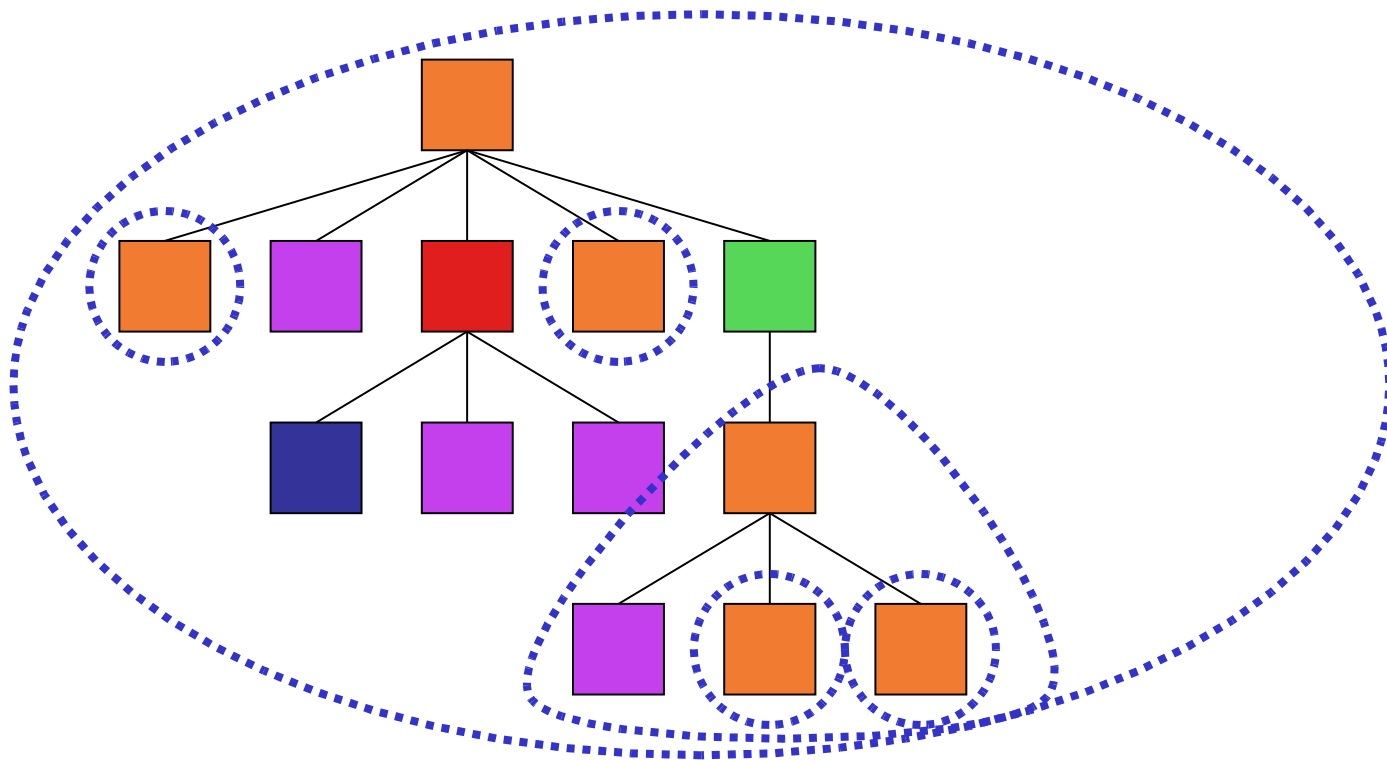
- Have some “mutator”
- Apply to each item

`traversal :: (a -> a) -> a -> a`

5. Bottom up
6. Top down – automatic
7. Top down – manual

# $\lambda$ Bottom-up traversal

`mapUnder :: (a -> a) -> a -> a`



# $\lambda$ The inc traversal

---

```
inc x = mapUnder f x
```

where

```
f (Val x) = Val (x+1)
```

```
f x = x
```

- Say the action (first line)
- Boilerplate is all do nothing

# Top-down queries

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- Bottom up is almost always best
- Sometimes information is pushed down
- Example: Remove negation of add

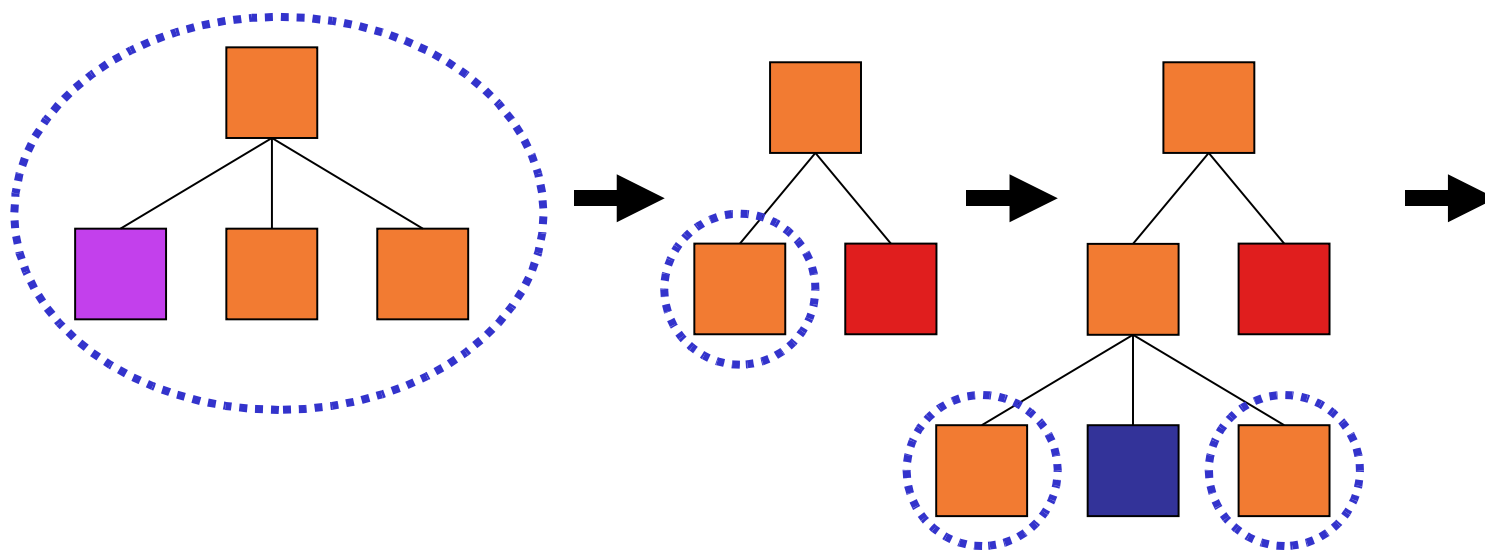
$$f \text{ (Neg (Add } x \ y)) = \text{Add (Neg } x) \text{ (Neg } y)$$

- Does not work,  $x$  may be Add

$$f \text{ (Neg (Add } x \ y)) = \\ \text{Add (} f \text{ (Neg } x) \text{) (} f \text{ (Neg } y) \text{)}$$

# $\lambda$ Top-down traversal

`mapOver :: (a -> a) -> a -> a`



Produces one element per call



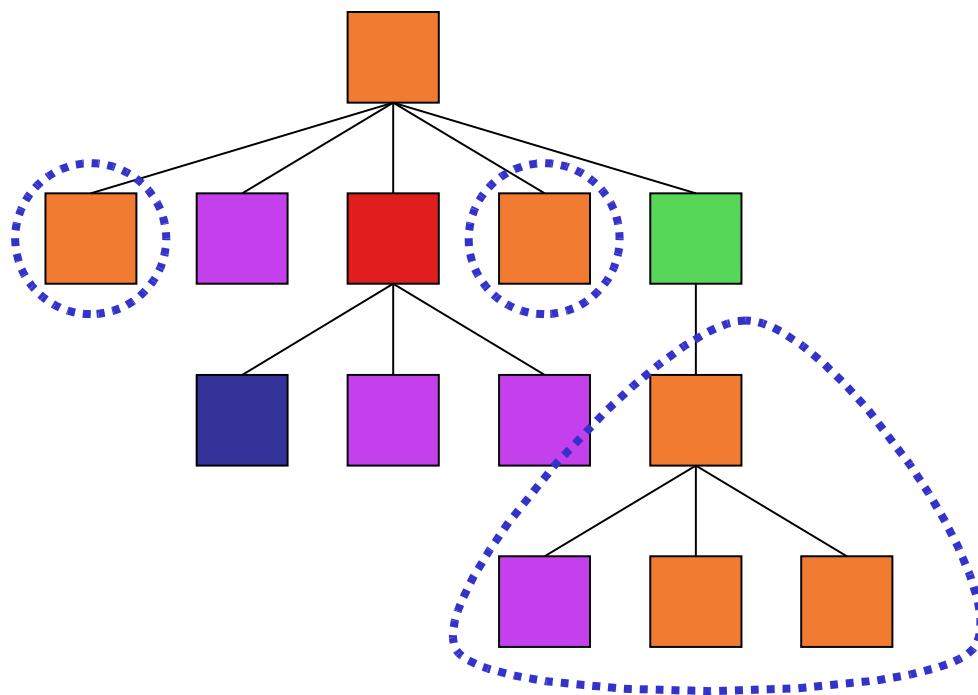
# $\lambda$ One element per call?

---

- Sometimes a traversal does not produce one element
- If zero made, need to explicitly continue
- In two made, wasted work
  
- Can write an explicit traversal

# $\lambda$ Top-down manual

compos  $:: (a \rightarrow a) \rightarrow a \rightarrow a$



# Compos

---

```
noneg (Neg (Add x y)) =  
    Add (noneg (Neg x)) (noneg (Neg y))  
noneg x = compos noneg x
```

- Compos does no recursion, leaves this to the user
- The user explicitly controls the flow

# $\lambda$ Other types of traversal

---

- Monadic variants of the above
- `allOverContext :: a -> [(a, a -> a)]`
  - Useful for doing something once
- `fold :: ([r] -> a) -> (x -> a -> r) -> x -> r`
  - `mapUnder` with a different return

# $\lambda$ The Challenge

---

Pick an operation  
Will code it up “live”

# $\lambda$ Traversals for *your* data

---

- Haskell has *type classes*
- `allOver :: Play a => a -> [a]`
- Each data structure has its own methods
- `allOver Expr /= allOver Program`

# $\lambda$ Minimal interface

---

- Writing 8+ traversals is annoying
- Can define all traversals in terms of one:

`replaceChildren :: x -> ([x], [x] -> x)`

- Get all children
- Change all children

# $\lambda$ Properties

---

```
replaceChildren :: x -> ([x], [x] -> x)
(children, generate) = replaceChildren x
```

- generate children == x
- @pre generate y  
length y == length children



# Some examples

---

`mapOver f x = gen (map (mapOver f) child)`  
where `(child,gen) = replaceChildren (f x)`

`mapUnder f x = f (gen child2)`  
where `(child,gen) = replaceChildren x`  
`child2 = map (mapUnder f) child`

`allOver x = x : concatMap allOver child`  
Where `(child,gen) = replaceChildren x`

# $\lambda$ Writing replaceChildren

---

- A little bit of thought
- Reasonably easy
  
- Using GHC, these instances can be derived automatically

# $\lambda$ Competitors: SYB + Compos

---

- Not Haskell 98, GHC only
- Use scary types...
- Compos
  - Provides compos operator and fold
- Scrap Your Boilerplate (SYB)
  - Very generic traversals

# $\lambda$ Compos

---

- Based on GADT's
- No support for bottom-up traversals

```
compos ::
```

```
(forall a. a -> m a) ->
```

```
(forall a b. m (a -> b) -> m a -> m b) ->
```

```
(forall a. t a -> m (t a)) ->
```

```
t c -> m (t c)
```

# $\lambda$ Scrap Your Boilerplate (SYB)

- Full generic traversals
- Based on similar idea of children
  - But is actual children, of different types!

```
gfoldl ::
```

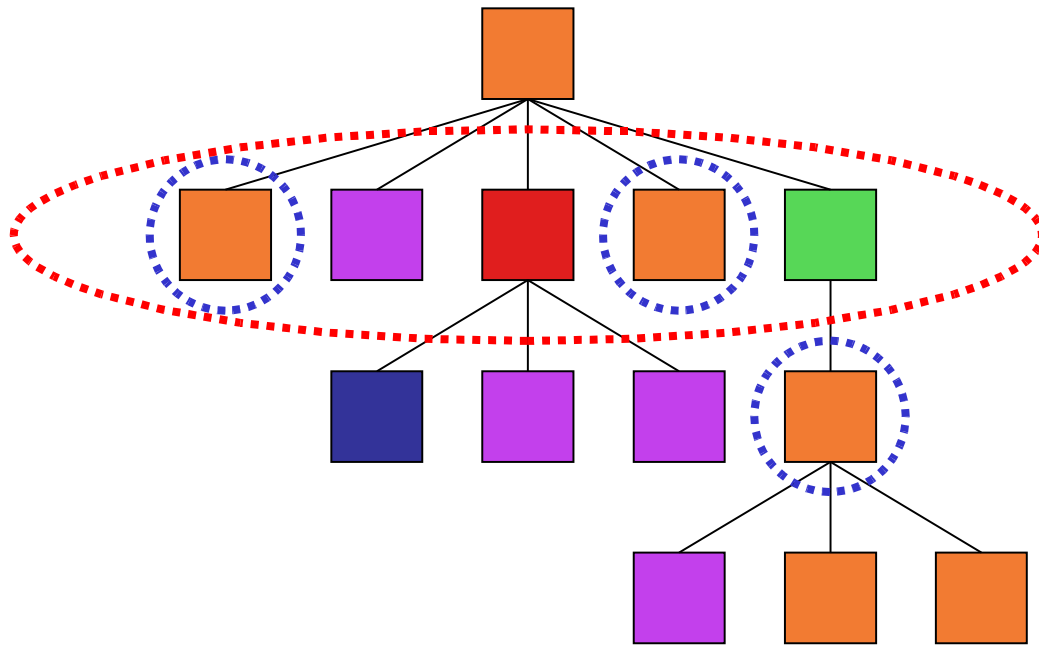
```
(forall a b. Term a => w (a -> b)
```

```
    -> a -> w b)
```

```
-> (forall g. g -> w g)
```

```
-> a -> w a
```

# $\lambda$ SYB vs Play, children



SYB  
Play

# $\lambda$ SYB continued

---

- Traversals are based on types:

```
0 `mkQ` f
```

```
f :: Expr -> Int
```

- mkQ converts a function on Expr, to a function on all types
- Then apply mkQ everywhere

# Paradise benchmark

```
salaryBill :: Company -> Float
salaryBill = everything (+) (0 `mkQ` bills)

bills :: Salary -> Float
bills (S f) = f
```

**SYB**

```
salaryBill c = case c of
  S s -> s
  _ -> composOpFold 0 (+) salaryBill c
```

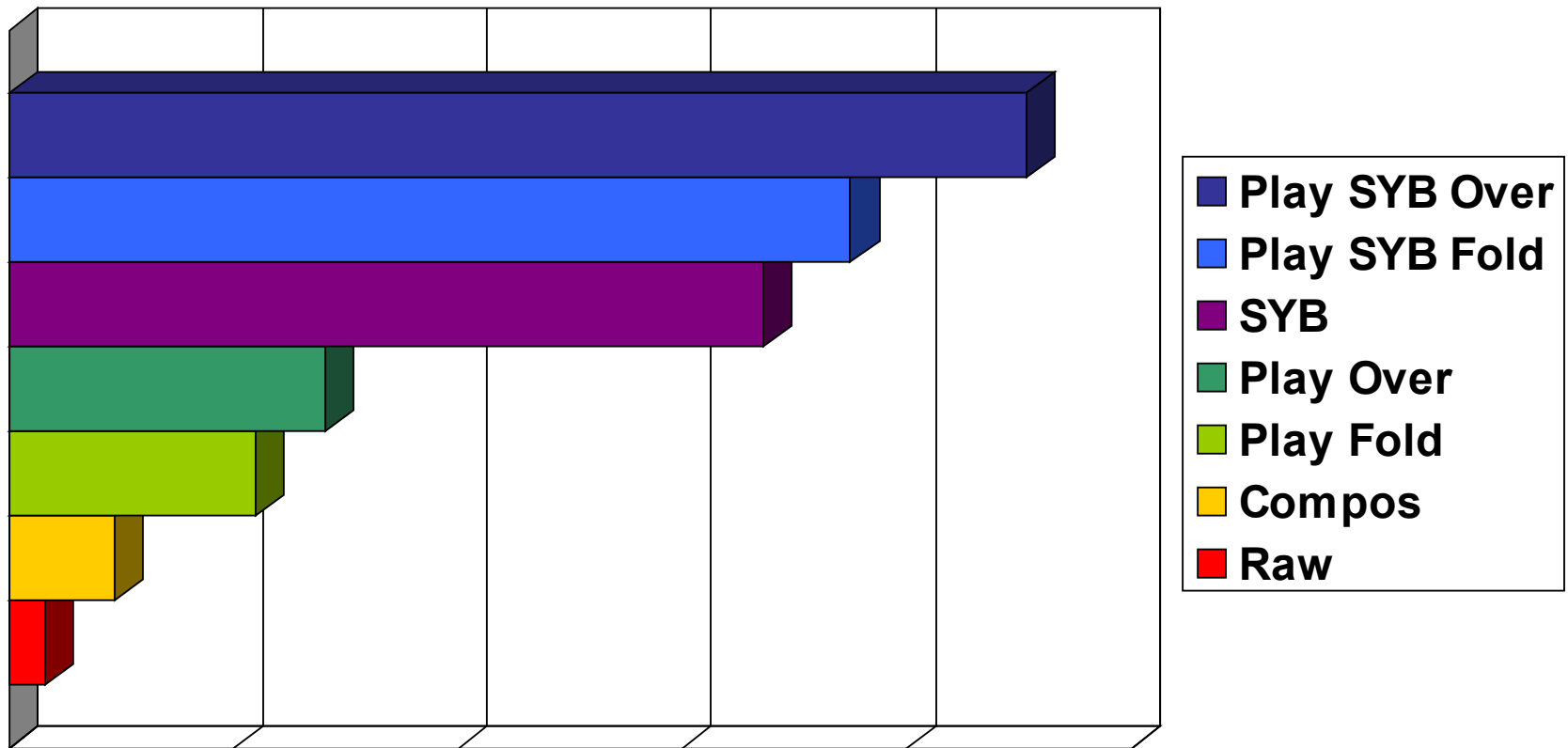
**Compos**

```
salaryBill x = sum [x | S x <- allOverEx x]
```

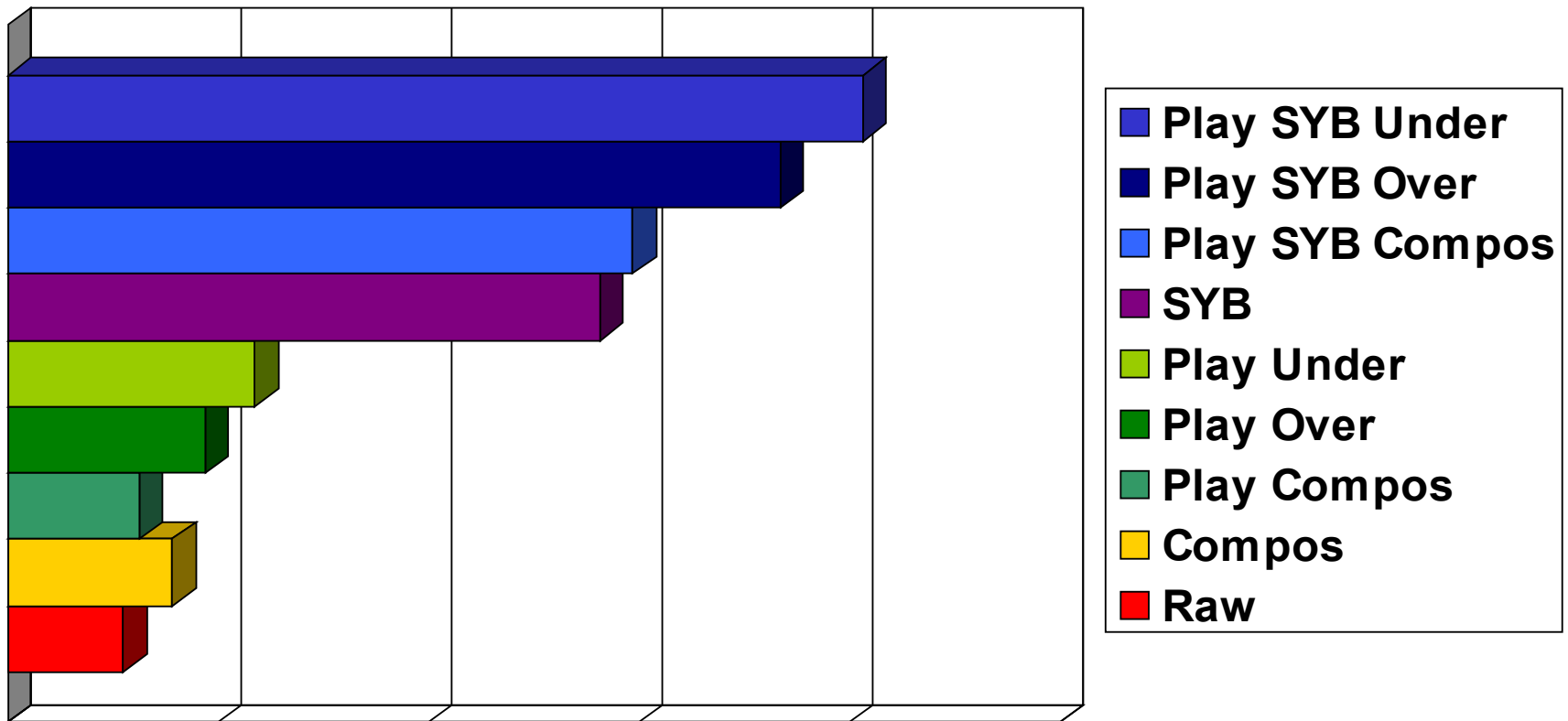
**Play**



# $\lambda$ Runtime cost - queries



# $\lambda$ Runtime cost - traversals



# $\lambda$ In the real world?

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- Used in Catch about 100 times
- Used in Yhc.Core library
- Used by other people
  - Yhc Javascript converter
  - Settings file converter

# $\lambda$ Conclusions

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- Generic operations with simple types
- Only 1 simple primitive
  
- If you only remember two operations:
  - allOver – queries
  - mapUnder – traversals